

GUJARAT TECHNOLOGICAL UNIVERSITY
BE – SEMESTER – VI (OLD).EXAMINATION – WINTER 2016

Subject Code: 160704**Date: 26/10/2016****Subject Name: Theory of Computation****Time: 10:30 AM to 01:00 PM****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1** (a) Define Mathematical Induction principle and prove that for any $n \geq 4$, $n! > 2^n$ **07**
 (b) Explain following **07**
 i. One to one and onto function
 ii. Properties of equivalence relation.
- Q.2** (a) Draw FA for each of the following RE. **07**
 i. $(0+1)^*(1+00)(0+1)^*$
 ii. $(0+1)^*(01+110)$
 iii. $(111+100)^*0$
 (b) Suppose that language L1 and L2 are the subsets given below. **07**
 $L1 = \{x \mid 00 \text{ is not a substring of } x\}$ $L2 = \{x \mid x \text{ ends with } 01\}$
 Draw FA for intersection L1 and L2
OR
- (b) For each of the RE draw NFA- Λ **07**
 i. $(0+1)^*(011+01010)(0+1)^*$ ii. $(0+1)(01)^*(011)^*$
- Q.3** (a) Explain pumping lemma and its application. **07**
 (b) For the following CFG, Find Chomsky normal form **07**
 $S \rightarrow AACD$ $A \rightarrow aAb \mid \Lambda$ $C \rightarrow aC \mid a$ $D \rightarrow aDa \mid bDb \mid \Lambda$
OR
- Q.3** (a) Find regular expression for following **07**
 i. Language of all strings containing exactly two 0's.
 ii. Language of all strings that begins or ends with 00 or 11.
 iii. Language of all strings in which every 0 is followed immediately by 11.
 (b) For the following CFG, Find Chomsky normal form **07**
 $S \rightarrow AaA \mid CA \mid BbB$ $A \rightarrow aaBa \mid CDA \mid aa \mid DC$ $B \rightarrow bB \mid bAB \mid bb \mid aS$
 $C \rightarrow Ca \mid bC \mid D$ $D \rightarrow bD \mid \Lambda$
- Q.4** (a) Write PDA for language of palindrome. Trace it with example. **07**
 (b) Explain Universal Turing Machine. **07**
OR
- Q.4** (a) Write PDA for the string with equal number of a's and b's. Trace it with example. **07**
 (b) Draw a TM to accept $\{ss \mid s \in \{a,b\}^*\}$. **07**
- Q.5** (a) Draw a TM to copy strings. **07**
 (b) Find minimum state FA recognizing the language corresponding to following RE. **07**
 i. $(0^*10+1^*0)(01)^*$ ii. $(010)^*1 + (1^*0)^*$
OR
- Q.5** (a) Explain Primitive recursive Function. **07**
 (b) Explain P, NP and NP complete problem. **07**
