

**GUJARAT TECHNOLOGICAL UNIVERSITY****BE SEMESTER – VI • EXAMINATION –Summer-2015****Subject Code: 160704****Date:14/05/2015****Subject Name: Theory of Computation****Time:10.30AM-01.00PM****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

**Q.1 (a)** Define Mathematical Induction Principle and Prove that for every  $n \geq 0$ , **07**

$$\sum_{i=0}^n i = n(n+1) / 2$$

**(b)** (i) Suppose that Languages L1 and L2 are the subsets given below. **05**

Where  $\Sigma = \{ 0, 1 \}$

L1 = { x | 00 is not a substring of x }

L2 = { x | x ends with 01 }

Draw FAs recognizing the following languages

(1) L1 - L2 (2) L1 ∩ L2

(ii) Show that the function  $f_1(x,y) = x + y$  is primitive recursive. **02**

**Q.2 (a)** Write definition of finite automata and draw FA for the strings: **07**

(i) The string in  $\{0,1\}^*$  ending in 10 or 11

(ii) The string corresponding to Regular expression  $\{11\}^*\{00\}^*$

**(b)** Define Context Free Grammar(CFG). Design CFG for Generating Following Language: **07**

(1) For Balanced Parenthesis

(2) Set of even length strings in  $\{a, b, c, d\}^*$  with two middle symbol equal.

**OR**

**(b)** Design an ambiguous grammar for if-then-else statement that also generates if-then statement. Re-write an equivalent unambiguous grammar. Prove that Grammar is Unambiguous by tracing “ic<sub>1</sub>tic<sub>2</sub>taea”. **07**

**Q.3 (a)** Convert NFA- $\wedge$  to NFA and DFA. Initial State: A , Final State: D **07**

| Q | $\delta(q, \wedge)$ | $\delta(q, 0)$ | $\delta(q, 1)$ |
|---|---------------------|----------------|----------------|
| A | {B}                 | {A}            | $\emptyset$    |
| B | {D}                 | {C}            | $\emptyset$    |
| C | $\emptyset$         | $\emptyset$    | {B}            |
| D | $\emptyset$         | {D}            | $\emptyset$    |

**(b)** Define Pumping Lemma for Regular Languages. Use Pumping Lemma to show that following languages are not regular. **07**

$L = \{ 0^n 1^{2n} / n > 0 \}$

$L = \{ ww^R / w \in \{0,1\}^* \}$

**OR**

**Q.3 (a)** Convert NFA- $\wedge$  to NFA and FA. Initial State: A , Final State: E **08**

| Q | $\delta(q, \wedge)$ | $\delta(q, 0)$ | $\delta(q, 1)$ |
|---|---------------------|----------------|----------------|
| A | {B,D}               | {A}            | $\emptyset$    |
| B | $\emptyset$         | {C}            | {E}            |
| C | $\emptyset$         | $\emptyset$    | {B}            |
| D | $\emptyset$         | {E}            | {D}            |
| E | $\emptyset$         | $\emptyset$    | $\emptyset$    |

**06**

**(b)** Find CFG from given PDA that accepts the language  $\{0^n 1^n\}$ . PDA is  $(Q, \Sigma, \Gamma, \delta, q, Z, F)$  where  $Q = \{q, r\}$ ,  $\Sigma = \{0, 1\}$ ,  $\Gamma = \{Z, X\}$ ,  $\delta$  is defined by:

| State | Input    | Stack | New State | Stack    |
|-------|----------|-------|-----------|----------|
| q     | 0        | Z     | q         | XZ       |
| q     | 0        | X     | q         | XX       |
| q     | 1        | X     | r         | $\wedge$ |
| r     | 1        | X     | r         | $\wedge$ |
| r     | $\wedge$ | Z     | r         | $\wedge$ |

**Q.4 (a)** (1) Given the Context Free Grammar G, find a CFG G' in Chomsky Normal Form generating  $L(G) - \{ \}$  **05**

$$S \rightarrow SS \mid A \mid B$$

$$A \rightarrow SS \mid AS \mid a$$

$$B \rightarrow \wedge$$

(2) Convert following CFG to PDA **02**

$$S \rightarrow 0S1 \mid 00 \mid 11$$

**(b)** For the language  $L = \{\text{set of strings over alphabet } \{a, b\} \text{ with exactly twice as many } a\text{'s as } b\text{'s}\}$  design a PDA (Push Down Automata) and trace it for the string "abaabbbaaaabaab" **07**

**OR**

**Q.4 (a)** Given the Context Free Grammar G, find a CFG G' in Chomsky Normal Form generating  $L(G) - \{ \}$  **07**

$$1) S \rightarrow aY \mid Ybb \mid Y$$

$$X \rightarrow \wedge \mid a$$

$$Y \rightarrow aXY \mid bb \mid XXa$$

$$2) S \rightarrow AA$$

$$A \rightarrow B \mid BB$$

$$B \rightarrow abB \mid b \mid bb$$

**(b)** For the language  $L = \{ a^i b^j c^k \mid i, j, k \geq 0 \text{ and } i + j = k \}$  design a PDA (Push Down Automata) and trace it for String "bbbbbbcccc" **07**

**Q.5 (a)** Design Turing Machine(TM) to accept Palindrome over  $\{a,b\}$ , even as well as odd. **08**

**(b)** Write Short Note on Following: **06**

(i) Universal TM

(ii) NP-Hard and NP-Complete Language

**OR**

**Q.5 (a)** Draw Turing Machine(TM) which recognizes words of the form  $\{ a^n b^n c^n \mid n \geq 1 \}$  **08**

**(b)** Write Short note on Following: **06**

(i) Halting Problem

(ii) Church Turing Thesis

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